Throughout this exam "graph" means simple graph, while "directed graph" will mean directed graph without multiple edges or loops.

Some problems on counting: possible relations and restrictions among: the number n of vertices m of edges k of components c - dimension of cycle space and the dimension of the cut space.

Definition and properties of connected vs unconnected graphs.

Incidence matrix D. As a mapping from the edge space to the vertex space. Properties of. Rank. Kernel. Properties of its transpose.

Parameterization of a line segment in a vector space, given two endpoints. Prüfer code.

Something about number of cycles, cuts, or spanning trees of a particular graph. A particular graph. I ask you to find m, n, k, c. Number of spanning trees.

Basis for cycle space. For cut space.